

1 **PDE Incorporated Multi-Feature Traffic Sign Detection**

2

3 **Chengbo Ai**

4 **Department of Civil and Environmental Engineering**

5 **Georgia Institute of Technology**

6 **210 Technology Circle**

7 **Savannah, GA 31407**

8 **Phone: (912) 660-4533**

9 **Email: chengbo.ai@gatech.edu**

10

11 **Yi-Chang (James) Tsai**

12 **Department of Civil and Environmental Engineering**

13 **Georgia Institute of Technology**

14 **210 Technology Circle**

15 **Savannah, GA 31407**

16 **Phone: (912) 966-6977**

17 **Email: james.tsai@ce.gatech.edu**

18

19 **Text words: 4423**

20 **Table: 1**

21 **Figures: 8**

22 **Total words: 6673**

1 **ABSTRACT**

2 Traffic signs are important transportation assets that are integrally related to roadway safety.
3 Current traffic sign inventory by transportation agencies is still a manual process that is labor
4 intensive and time consuming. A generalized traffic sign detection algorithm with a
5 reasonably good performance has been developed using multiple features to automatically
6 detect signs. However, correctly detecting signs with discontinuous boundaries remains a
7 challenge that lead to false negatives. To address the issue, a partial differential equation
8 (PDE) method, which is a region-based active contour model, is proposed. A new energy
9 function incorporated with a location probability distribution function (PDF) is proposed for
10 the active contour. The contributions of this paper include the following: 1) proposes a PDE
11 method to improve discontinuous sign detection; 2) proposes a location PDF incorporated
12 energy function component to provide a more accurate contour initial guess; 3) the new
13 method is integrated into existing system framework without affecting existing methods. The
14 video-log image data from the City of Nashville are used to perform the test. Using the new
15 method, 24 out of 26 images with a discontinuity issue are correctly detected, and 607 images
16 from a road segment are tested to compare the performance of the enhanced system and the
17 previous system. Results show that false negative rate has been reduced 6.8% from 21.1%
18 while the false positive rate has increased 1.2% from 11.2% with the enhanced system. The
19 results show that incorporating the proposed PDE method to develop an enhanced sign
20 detection system is promising. Future research for incorporating additional distinct features
21 into the generalized algorithm is also discussed.

1. INTRODUCTION

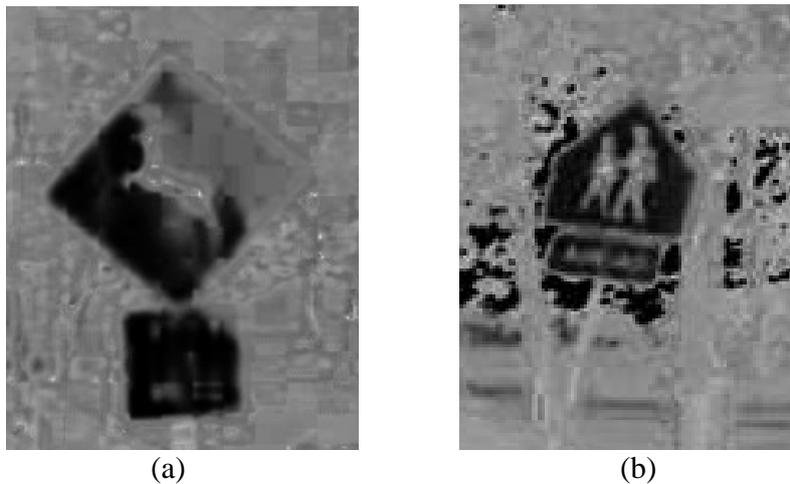
As one of the most important traffic control devices defined in the Manual of Unique Traffic Control Devices (MUTCD), a traffic sign's existence, location, and condition inevitably affect transportation mobility and safety, as stated in the revised MUTCD (2003). Thus, different transportation agencies, such as state departments of transportation (DOTs), are dedicating their workforce to traffic sign inventory and condition assessment. Traditionally, transportation agencies manually collect traffic sign data in the field, which is time consuming, costly, and dangerous. Some transportation agencies collect traffic sign data in the office by manually reviewing video-log images. For example, Georgia has approximately 118,000 centerline miles of roadway. According to the current data collection practice, 100 images per mile, the Georgia Department of Transportation has more than 11 million roadway video-log images. Reviewing these images one frame at a time is extremely time consuming and costly.

To reduce the cost and time of traffic sign inventory, much effort has been expended to develop algorithms for automatic traffic sign detection and recognition. These algorithms try to extract a traffic sign using distinct features that uniquely define different types of traffic signs. Some algorithms use color (Ritter, 1995) or shape (Schiekel, 1999; Gil-Jimenez, 2005; Kim, 2005; Tsai and Wu, 2002) for traffic sign detection and recognition, while others combine these two features (An, 1998; Miura, 2002; Gao, 2003; Zhu, 2006; Wu and Tsai, 2006). In addition, geometrical, physical, and text/symbol features are used for traffic sign detection (Liu, 2007; Wu and Tsai, 2005). To extract traffic sign features, methods like the Support Vector Machine (SVM) and the Neural Network (NN) are used (Gil-Jimenez, 2005; Zhu, 2006). In recent years, the Haar feature-based Ada-boost method, which was originally applied in face detection (Bahlmann, 2005; Silapachote, 2005), was developed for traffic sign detection and recognition. However, the following challenges still remain:

1. For traffic sign inventory, more than 670 types of traffic signs with different sizes, shapes, colors, and legends are specified in the MUTCD. It is a challenge to develop a generalized automatic traffic sign detection algorithm to process all of these types;
2. To make an automatic process practical, the automatic traffic sign detection algorithm should be accurate with an acceptable false negative rate that reflects reliability and a reasonable false positive rate that reflects productivity;
3. The algorithms should be robust enough to detect images that are captured under different lighting conditions, e.g. backlight and sun glare, and varying environmental conditions, e.g. foggy weather and rain showers;
4. Because there is no standard among transportation agencies, the algorithms should be adaptive enough to process images captured by different camera configurations, e.g. different camera resolution, orientation, etc.

To address these challenges in the existing automatic traffic sign detection method, a novel, generalized, multi-feature traffic sign detection algorithm is developed. The performance test shows a reasonably good result (Tsai et al, 2009; Tsai and Wang, 2008) in terms of traffic sign detection rates. A new proposed statistical color model (SCM) is first applied to determine and classify the color probability of each image. The Canny edge detection method with Sobel operator is then applied (Canny, 1986; Abdou, 1979) to extract all the edges in the segmented color images. Finally, a contour-smoothing and approximation algorithm is applied to extract all the possible polygons (Douglas, 1973).

1 Though the algorithm performed well in several large-scale tests, e.g. on more than
2 37,000 images collected by Louisiana Department of Transportation and Development
3 (LaDOTD), challenges remain. After analyzing the false negatives in the test results, images
4 with discontinuous sign boundaries are identified as one of the most difficult technical
5 challenges for correctly extracting traffic signs. Figures 1(a) and 1(b) show two traffic signs
6 that are not detected in the existing system due to the discontinuous sign boundary. In Figure
7 1(a), the upper left portion of the deer warning sign (W11-3) merges into the background,
8 making the boundary indistinguishable. In Figure 1(b), the school sign shares the same
9 boundary with the “ahead” legend (W16-9p); the shared boundary does not have a consistent
10 intensity and does not separate the two adjacent traffic signs clearly.
11



12
13
14 **FIGURE 1 Two Cropped Color Segmented Images with Discontinuity Issues.**
15

16 The objective of this paper is to improve the performance of contour extraction for
17 traffic signs with discontinuous boundaries and to reduce the false negative rate without
18 adding excessive false positives. Considering the strong capability of active contour in
19 boundary extraction and shape description (Kass, 1988), this partial differential equation
20 (PDE) method is introduced and incorporated in the current automatic traffic sign detection
21 system. In this paper, a new, region-based active contour model is formulated by
22 incorporating the location probability distribution function (PDF) information and curve
23 length constraint. Based on the formulated energy function, the contour will evolve within the
24 color-segmented images and, finally, locate the traffic sign boundary, even when sign
25 boundaries are discontinuous. The location PDF information is implicitly embedded in the
26 energy function, so the initial guess can be improved. Also, the curve length constraint, as a
27 global iteration termination criterion, is included to prevent excessive iteration during the
28 contour evolvment and to separate compound traffic signs.

29 This paper is organized into several sections. This section introduces the need for an
30 automatic traffic sign detection system. The undetected traffic signs with discontinuous
31 boundaries are identified, and a region-based active contour is proposed to improve the
32 system. Section 2 presents the methodology for integrating the region-based active contour
33 into the existing system. The formulation of a location PDF incorporated region-based active
34 contour to enhance the initial guess is presented. Section 3 presents the test results and shows
35 the improvement in detecting traffic signs with discontinuous sign boundaries and also shows

1 the robustness of active contour initial region guesses. The assessment and analysis of the
2 results is also presented. The last section presents the conclusion. Recommendations for
3 further improvement of this PDE method, as well as the improvements for the entire detection
4 system, are also presented.

5 **2. METHODOLOGY**

6 **2.1 Introduction of Active Contour**

7 Active contours, or snakes (Kass, 1988), are computer-generated curves that move within
8 images to find object boundaries. They are often used in computer vision and image analysis
9 to detect and locate objects and to describe their shapes. They are widely used in medical
10 image processing, e.g. in automatically extracting MRI images of cancer. An edge-based
11 active contour approach (Malladi, 1995; Chenyang, 1998) and a region-based active contour
12 approach (Chan, 2001) are the two most popular formulations. With a good energy function
13 and initial guess, the active contour method is capable of accurately extracting the boundary
14 around the target object. There are two major challenges existing in all the active contour
15 methods:

- 16 1. Initial guess. The active contour method requires an initial guess to accelerate the
17 contour-evolving process and obtain the target contour accurately. This is a challenge,
18 especially when the image has a complicated background and heavy noise, e.g. in
19 natural-scene images;
- 20 2. Iteration termination. When performing of the active contour, the contour will stop
21 evolving when the preset iteration number is achieved or the iteration converges with
22 certain errors. However, the decision to terminate iteration is still a challenge and,
23 most of the time, is handled case by case;

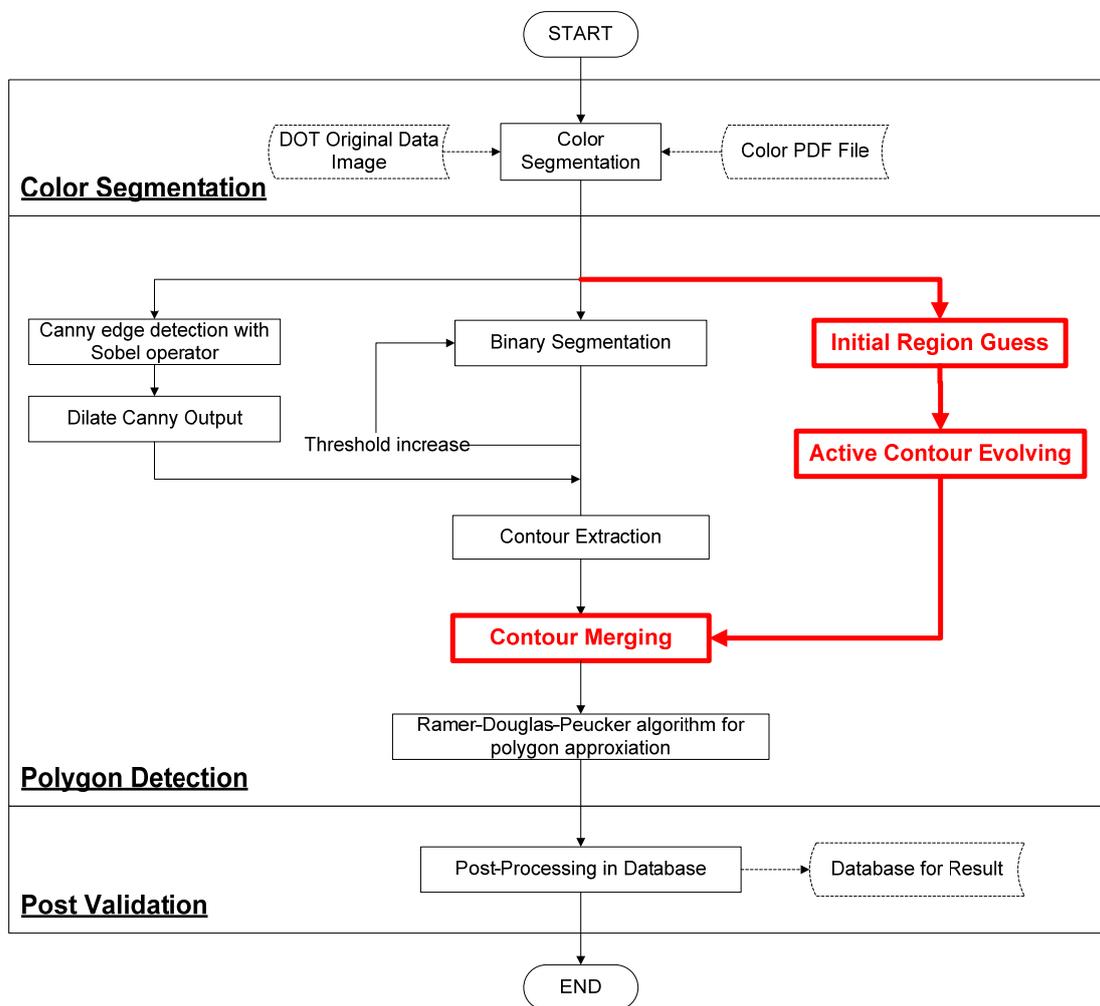
24 Due to these two major challenges, to the best knowledge of the authors, there is little
25 research that directly applies active contour methods to traffic sign detection or other natural
26 scene object extraction problems. Quan and Mohr (1990) apply a geodesic active contour
27 directly to the collected raw image and get some preliminary results in traffic sign detection.
28 Paulo (2008) presents an active contour-based method with a selected dataset to extract the
29 legend and icon from a traffic sign. Several methods are proposed based on geodesic active
30 contour and optical flow analysis in sequential images with static backgrounds to deal with
31 the application of vehicle extraction, pedestrian extraction, and tracking, etc (Andrade, 2005;
32 Coifman, 1998). In this paper, the initial guess and the iteration termination challenges are
33 dealt with by using the newly proposed hybrid energy function.

34 To detect a traffic sign with discontinuous boundaries, the region-based, active
35 contour model is selected. The region-based active contour is first proposed by Chan and
36 Vese (2001). It is considered as the “active contour without edge.” Similar to the edge-based
37 active contour, the problem is considered as an energy-minimization problem. The difference
38 is that instead of using an energy function with an edge-sensitive element $|\nabla I|$, the region-
39 based active contour energy function incorporates the regional information inside the contour
40 and the information outside the contour, which is much more robust than the noise and local
41 perturbation. Compared with the edge-based active contour, the region-based contour
42 performs much better when the input image has a pattern that includes two different
43 intensities throughout the image, especially the images with heavy noise. The color-
44 segmented images by SCM provide a preferable input for the region-based active contour,

1 which shows that the foreground traffic sign region has a higher intensity while the
 2 background region has a lower one.
 3

4 **2.2 Active contour incorporated traffic sign detection algorithm framework**

5 In this paper, the newly proposed active contour algorithm is designed as an enhancement of
 6 the existing system. The existing system consists of three major procedures, including color
 7 segmentation, polygon detection, and polygon validation. As mentioned in the previous
 8 section, the enhancement algorithm, using active contour, is applied in the polygon detection
 9 procedure to extract the previously omitted contours. An enhanced traffic sign detection
 10 algorithm framework is formulated by incorporating the active contour algorithm in parallel
 11 into the existing polygon detection procedure.
 12



13
 14
 15
 16
 17
 18

FIGURE 2 Framework of Current Detection System and Enhanced Detection System.

In the existing algorithm for polygon detection, the Canny edge detection and multi-step binarization methods are applied to the color segmented image inputs to extract the

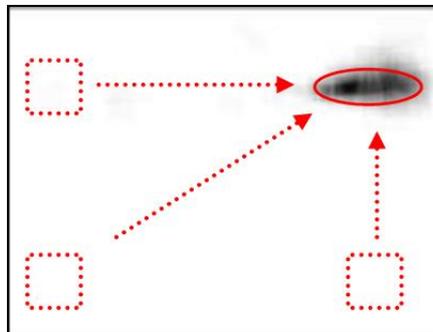
1 contours, as shown in Figure 2. In the enhanced algorithm, the active contour algorithm is
 2 appended, as shown in Figure 2 (in bold), to the existing algorithm. Color segmented images
 3 are separately input through three different contour extraction paths. For the two paths in the
 4 existing system, edges are first detected, and then the contours are retrieved using
 5 interpolation of the edge points. For the active contour path, according to the formulated
 6 energy function, the contours are directly extracted. All the contours obtained from the
 7 existing branches and active contour branch are merged into the same data storage as a pool
 8 of all the contours, i.e. sequences of contour point vectors. Finally, the polygon approximation
 9 continues with all of those contours and formulates the polygons.

10 The design of the parallel structure in the enhanced system maintains the strength of
 11 the existing system and further utilizes the capability of active contour. Thus, the contours of
 12 the undetected traffic signs with discontinuous boundaries can be extracted and detected as
 13 traffic signs. The parallel algorithm design also maintains the capability of processing large
 14 numbers of images without intermediate inputs, which makes the system ready for practice
 15 use.

16 2.3 Formulation of Region-Based Active Contour

17 Under the new formulation of the enhanced system, a new energy function is needed for the
 18 region-based active contour, which can be used to trace discontinuous boundaries but not add
 19 excessive contours that do not belong to the traffic sign. Based on these considerations, the
 20 new region-based active contour is formulated with a hybrid energy function consisting of
 21 three sub-energy components: location PDF energy, color segmented image energy, and
 22 global curve length. These sub-energy components are designed to force the active contour to
 23 trace the traffic sign boundary locally and to improve the initial guess and global termination
 24 in the general active contour method.

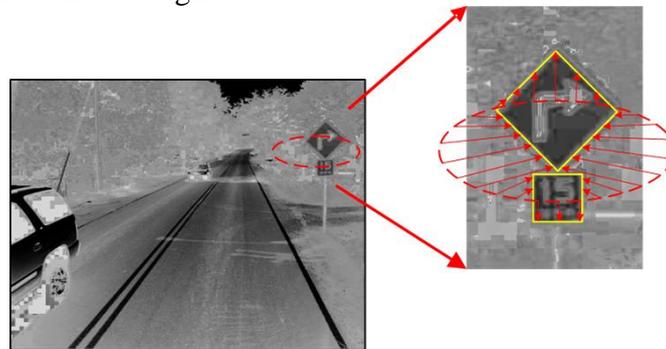
- 26 • Energy 1: Location PDF energy. The location PDF (Tsai et al, 2009) energy serves as
 27 an implicit, initial region guess of the active contour. It is formulated within the
 28 location PDF bitmap image. As shown in Figure 3, a location PDF bitmap generated
 29 from 1000 video-log images collected by the City of Nashville is used. The dotted
 30 squares indicate several random initial guesses, and the arrows indicate the contours'
 31 evolving directions. This energy controls the global evolvment of the contour moving
 32 towards the high-likelihood area of traffic sign's occurrence, defined by the location
 33 PDF.



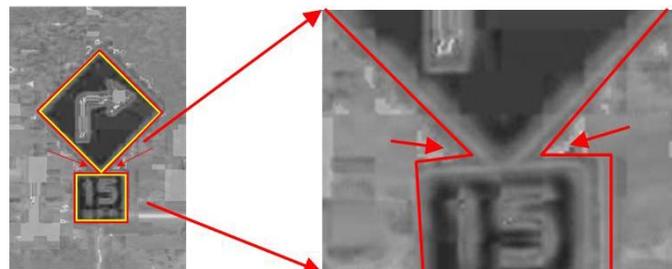
35
 36 **FIGURE 3 Contour Evolvment Forced by Location PDF Energy.**

1
2
3
4
5
6
7
8
9
10
11
12
13
14

- Energy 2: Color segmented image energy. This energy serves as the basic region-based active contour energy. It is formulated over the color-segmented image input. As shown in Figure 4(a), after the global evolvment controlled by Energy 1, most of the time the contours have already been located at the upper right area of the images, where they will be most likely to occur. The circle indicates the contour developed following Energy 1. This energy controls the local evolvment of the contour along the traffic sign boundary. The energy will pull the contour towards the traffic sign boundary from the outside when the curve is out of the traffic sign region, and the energy will push the contour towards the traffic sign boundary from the inside when the curve is across or within the traffic sign region. Specially, shown in Figure 4(b), when there are two traffic signs sharing certain parts of the boundary, this energy will trace the gap of the boundary between the traffic signs and, from outside, pushes the curve to separate the two signs.



(a)



(b)

15
16
17

FIGURE 4 Contour Evolvment Forced by Color Segmented Image Energy.

18
19
20
21
22
23
24
25
26
27
28
29
30

- Energy 3: global curve length energy. The global curve length serves as a global iteration termination criterion. When the curve length is too long, this component becomes a dominant energy of the total energy, which prevents the contour from continuously evolving and blowing up, especially when the iteration number is set as a large one. Also, this energy could help to separate one big curve into several smaller ones when processing the compound traffic signs sharing the same boundary;

Each of the energy components is shown as below in Equation (1):

$$E = \lambda \cdot \left[\int_{R_{PDF}} (I_{PDF} - u_{PDF})^2 dA + \int_{R_{PDF}^c} (I_{PDF} - v_{PDF})^2 dA \right] + (1 - \lambda) \cdot \left[\int_{R_{Original}} (I_{Original} - u_{Original})^2 dA + \int_{R_{Original}^c} (I_{Original} - v_{Original})^2 dA \right] + \mu |c| \quad (1)$$

where

$I_{Original}$ is the color segmented video-log images,

I_{PDF} is the location PDF bitmap;

λ is a scaling parameter to balance the two sub components, e.g. 0.15;

u and v are the average intensity inside of the contour and outside of the contour respectively.

The suffix indicates the value is from the color segmented video-log image or the location PDF bitmap.

This approach can be implemented using the level set method; the energy function can be rewritten using Heaviside function H as

$$E(u_{Original}, v_{Original}, u_{PDF}, v_{PDF}, \phi) = \lambda \cdot \left[\int_{R_{PDF}} |I_{PDF} - u_{PDF}|^2 H(\phi) dA + \int_{R_{PDF}^c} |I_{PDF} - v_{PDF}|^2 H(\phi) dA \right] + (1 - \lambda) \cdot \left[\int_{R_{Original}} |I_{Original} - u_{Original}|^2 H(\phi) dA + \int_{R_{Original}^c} |I_{Original} - v_{Original}|^2 H(\phi) dA \right] + \mu \int_R |\nabla(H(\phi))| \quad (2)$$

where

ϕ is the level set function;

H is the Heaviside function.

To minimize the energy function E with respect to $u_{Original}$, u_{PDF} , $v_{Original}$, v_{PDF} and ϕ , we need to solve the equations (3) and (4):

$$u_X = \frac{\int_{R_X} I_X H(\phi) dA}{\int_{R_X} H(\phi) dA} \quad v_X = \frac{\int_{R_X} I_X (1 - H(\phi)) dA}{\int_{R_X} (1 - H(\phi)) dA} \quad X = Original, PDF \quad (3)$$

$$\frac{\partial \phi}{\partial t} = \delta_\epsilon(\phi) [-(1 - \lambda) |I_{PDF} - u_{PDF}|^2 + (1 - \lambda) |I_{PDF} - v_{PDF}|^2 - \lambda |I_{Original} - u_{Original}|^2 + \lambda |I_{Original} - v_{Original}|^2] + \mu \operatorname{div} \left(\frac{\nabla \phi}{|\nabla \phi|} \right) = 0 \quad (4)$$

where

$\delta_\epsilon = H'_\epsilon$, that H_ϵ is a C^1 -approximation of H . These equations can then be implemented using standard finite difference (Ames 1977).

The feature of the location PDF provides extra information of the potential traffic sign occurrence location in the image plane, which can be used to guide the evolvement of the active contour. By formulating a hybrid energy function with the global information from the

1 location PDF and the local information from the color-segmented video-log image, the
2 moving trajectory of the contour evolvment follows the behavior even when the initial guess
3 region is randomly selected:

- 4 • If the preset initial guess happens to be at the region with higher probability to find a
5 traffic sign, the location PDF energy, defined above as Energy 1, component has less
6 effect on the total energy, so the dominant component of the energy is shifted to the
7 color segmented image energy, defined above as Energy 2. The contour will evolve
8 locally to trace the traffic sign region's boundary, which behaves like the basic region-
9 based active contour;
- 10 • If the preset initial guess happens to be at the region with a lower probability of
11 finding a traffic sign, the location PDF related energy has a dominant decision that
12 directs the contour moving towards the higher probability area, and the color
13 segmented related energy will not affect the total energy much until the contour
14 arrives at the region with high probability to find a traffic sign;
- 15 • Eventually, the global curve length energy, defined above as Energy 3, will contour
16 the overall contour length and terminate the evolvment. According to the observation
17 of a large set of video-log images, it is noticed that the coverage of a traffic sign in a
18 video-log image is no more than $\frac{1}{4}$ of the image. Therefore a preferred length can be
19 defined, e.g. 1200 pixels.

20 3. TESTS AND RESULTS

21 In this paper, three test results are presented. First, the robustness of the initial guesses is
22 tested with different initial region guesses. Second, a number of undetected traffic signs with
23 discontinuous boundaries are tested. Finally, a general performance test is performed after
24 incorporating the region based active contour into the existing system. For the robustness test
25 with different initial region guesses, 10 images are tested with 4 initial guesses each. For the
26 performance test in processing traffic signs with discontinuous boundaries, a selected set of
27 26 images containing traffic signs that have discontinuous boundaries is prepared and tested.
28 For the general performance test, 607 video-log images from a complete segment provided by
29 the City of Nashville, with a resolution of 1300*1030, are used. In the 607 images, there are
30 474 negative images that do not contain traffic signs and 133 positive images that contain
31 traffic signs with different sizes, colors, shapes, and conditions. In the 133 positive images, 7
32 images with discontinuity issues are from the 26 images used in the previous test.

33 3.1 Robustness test of different initial region guesses

34 In this test, 10 selected images are processed by the enhanced system. Each image is tested
35 four times with different initial guess regions, i.e. four corners of the image. The initial guess
36 region is set up as a 30*30 square pixels. A location PDF bitmap image generated from 1000
37 video-log images provided by the City of Nashville is used as another input. Figure 5 shows
38 the bitmap pattern of the location PDF. The dark area indicates a high probability of traffic
39 sign occurrence, while the bright area indicates the opposite. As mentioned in the energy
40 formulation, the location PDF is derived using the actual sign location in the roadway video-
41 log images. The four squares indicate four initial guesses for the designed region based active
42 contour.
43

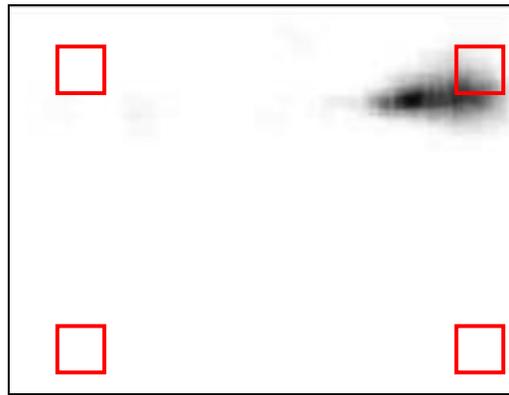


FIGURE 5 Location PDF Bitmap Image and Four Initial Guesses.

The results show that by following the energy decreasing direction proposed in Section 2, the contours converge to the same area, i.e. top-right of the image, and extract the traffic sign correctly, regardless of the different initial guesses. Figure 6 shows an example of the contour converging to the same location with different initial guess regions. It is observed that after the iterations, the initial guess contour region, which is the square, either on the upper left or on the bottom left, converges to the traffic sign region and finally traces the traffic sign boundary correctly.

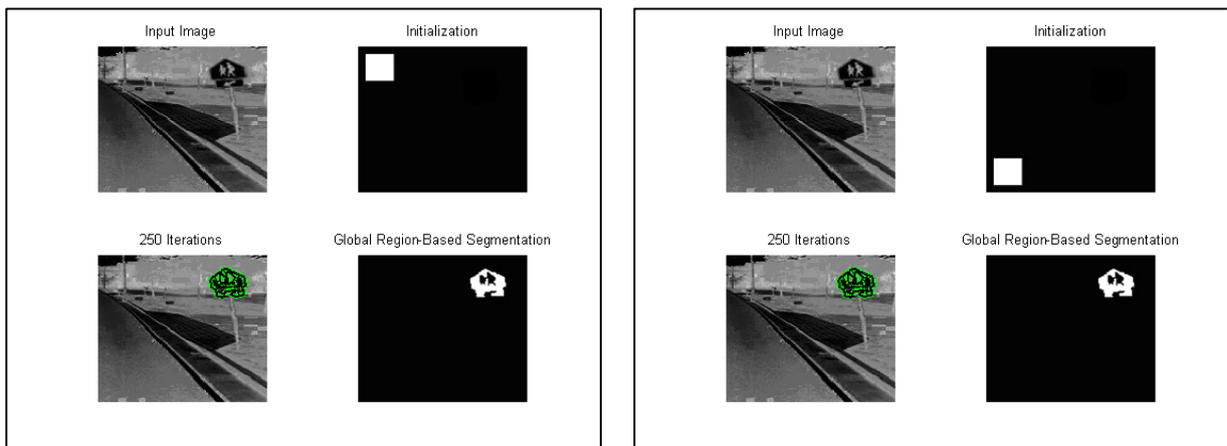


FIGURE 6 Result in Testing Robustness of Different Initial Guess Regions.

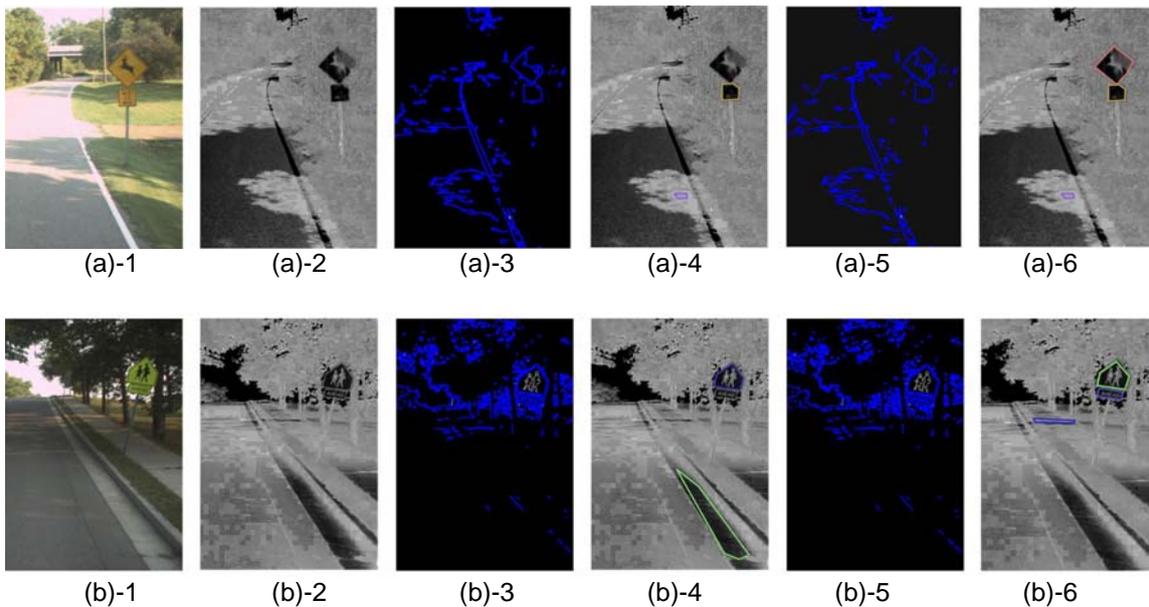
3.2 Discontinuity image detection

In this test, 26 selected images with discontinuity issues are tested. The 26 images are first processed by the existing system, and the results show that the existing system cannot correctly detect them, which causes false negatives. The enhanced system is applied. Of the images with traffic signs that have discontinuous boundaries, 24 out of 26 are correctly detected by the enhanced system. Figure 7 shows some of the results. It can be observed that the following discontinuity cases are successfully detected:

- Broken traffic signs due to the shadows or light glaring, shown in Figure 7(a). After color segmentation, the image is decomposed in different colors, shown in 7(a)-2, however, the upper right region of the deer sign (W11-3) is decomposed as a different color from the rest of the sign, which breaks the traffic sign region into two pieces, as

1 well as the boundary. In 7(a)-3, it is shown that with the color segmentation results,
 2 the boundary of the deer sign is not completely extracted, which produces an
 3 undetected case shown in 7(a)-4. After applying the proposed active contour algorithm,
 4 the boundary is completely extracted with the shape of the diamond, shown in 7(a)-5,
 5 which helps to correctly detect this traffic sign, as shown in 7(a)-6;

- 6 • Compound traffic signs sharing the same boundary, as shown in Figure 7(b). After
 7 color segmentation ,the image is decomposed in different colors shown in 7(b)-2;
 8 however, there are two traffic sign in this image sharing the same boundary and the
 9 boundary does not clearly separate the two traffic signs which have an inconsistent
 10 intensity along the boundary. In 7(b)-3, it is show that due to the inconsistency
 11 intensity along the in-common boundary, the contours extracted do not close the
 12 boundary of both of the traffic sign; instead, only the upper school sign’s contour is
 13 closed, while the lower “ahead” sign (W16-9p) has a non-close contour. Thus, as
 14 shown in 7(b)-4, only the school sign can be extracted, but the “ahead” sign is
 15 undetected. After applying the proposed active contour algorithm, the boundary is
 16 completely extracted for both of the traffic signs, shown in 7(b)-5; finally, both of the
 17 signs can be correctly detected shown in 7(b)-6.



22 **FIGURE 7 Result Comparison of Images with Discontinuity Issues.**

23 (From left to right, original image, color segmented image, extracted contour with existing algorithm, polygon
 24 detection result with existing algorithm, extracted contour with enhance algorithm, polygon detection result with
 25 enhanced algorithm)
 26
 27
 28

29 The results show the enhanced system performs well in detecting traffic signs that
 30 have discontinuity issues. However, there are still some cases for which the enhanced system
 31 has challenges to handle. Figure 8 shows the 2 unhandled cases. In Figure 8(a), the original
 32 image has a similar foreground and background in the color space, which causes
 33 undistinguished color segmentation. When the region-based active contour is applied in that
 34 area, the contour region will blow up, as shown. An improvement in color segmentation might
 35 be needed for such cases.

1 In this paper, a new region-based active contour model is presented to enhance the existing
2 automatic traffic sign detection system by improving contour extraction performance when
3 the input color segmented images contain traffic signs with discontinuous boundary. The
4 major contributions of this paper are as follows:

- 5 • Traffic signs with discontinuous boundaries can be detected by the new region-based
6 active contour method. The test result shows that 24 out of 26 traffic signs with
7 discontinuous boundaries that could not be detected previously are correctly detected;
- 8 • The location PDF information is implicitly embedded in the new region-based active
9 contour energy function and demonstrates robustness in the contour initial guesses.
10 The test results show that all of the contours converge to the traffic sign region
11 regardless of different initial guesses.
- 12 • The new, region-based active contour algorithm is incorporated into the current traffic
13 sign detection system. The enhanced system demonstrates a promising performance in
14 traffic sign detection. The test results show that an overall 14.3% false negative rate is
15 achieved by using the enhanced system compared with the 21.1% false negative rate
16 by using the existing system. Also, the overall 14.3% false positive rate is achieved
17 compared with a 12.9% false positive rate, which is only 1.7% more than the existing
18 system.

19 In future work, the following studies on the PDE method, i.e. active contour, are
20 recommended:

- 21 1. A complete performance test with a larger number of images is recommended so that
22 an more comprehensive assessment of the whole system performance can be
23 conducted;
- 24 2. Other robust initial region guesses can be explored and applied to the system, such as
25 multiple initial guess regions, etc. Also, other global iteration termination criteria can
26 be applied instead of the curve length used in this paper's enhancement, e.g. the area
27 of the contour region, etc.
- 28 3. An enhanced color model is recommended for color segmentation, especially when
29 the images contain the foreground traffic sign color and the background color that are
30 visually undistinguishable;
- 31 4. A reliable polygon validation method is recommended to further reduce the extracted
32 candidate traffic sign regions after polygon detection using other traffic sign features,
33 e.g. validation of the legend shapes, etc., so that the false positive rate can be further
34 reduced;
- 35 5. Multiple sensing technologies are recommended for incorporation into the system, so
36 that some invisible features can be utilized, such as depth information by using
37 LiDAR (Light Detection and Ranging), etc.

References

1. Manual on Uniform Traffic Control Device, 2003 Edition with Rev. 1 and Rev. 2, Part 2 Signs, Federal Highway Administration, Washington, D. C., 2001.
2. Ritter, W., F. Stein, and R. Janssen. Traffic Sign Recognition Using Color Information. *Mathematical and Computer Modeling*, Vol. 22 No. 4-7, 1995, pp. 149.
3. Schiekkel, C. A fast traffic sign recognition algorithm for gray value images. *Computer Analysis of Images and Patterns*, Vol. 1689, 1999, pp. 588-595.
4. Gil-Jimenez, P., S. Lafuente-Arroyo, S. Maldonado-Bascon, and H. Gomez-Moreno. Shape classification algorithm using support vector machines for traffic sign recognition. *Proceedings on Computational Intelligence and Bioinspired Systems*, Vol. 3512, 2005, pp. 873-880.
5. Kim, J. W., K. H. Jung, and C. C. Hyun. A study on an efficient sign recognition algorithm for a ubiquitous traffic system on DSP. *Computational Science and Its Applications - Iccsa 2005, Part 1*, Vol. 3480, 2005, pp. 1177-1186.
6. Tsai, Y. and Wu, J. Shape- and texture-based 1-D image processing algorithm for real-time stop sign road inventory data collection. *Journal of Intelligent Transportation System*, Vol. 7 No. 3-4, 2002, pp. 213-234.
7. An, J. H., and T. Y. Choi. Dominant color transform and circular pattern vector for traffic sign detection and recognition. *Ieice Transactions on Fundamentals of Electronics Communications and Computer Sciences*, Vol. E81a, No. 6, 1998, pp. 1128-1135.
8. Miura, J., T. Kanda, S. Nakatani, and Y. Shirai. An active vision system for on-line traffic sign recognition. *Ieice Transactions on Information and Systems*, Vol. E85d, No. 11, 2002, pp. 784-1792.
9. Gao, X. W., L. Podladchikova, and D. Shaposhnikov. Application of vision models to traffic sign recognition. *Artificial Neural Networks and Neural Information Processing Ican/Iconip 2003*, Vol. 2714, 2003, pp. 1100-1105.
10. Zhu, S. D., Y. Zhang, and X. F. Lu. Detection for triangle traffic sign based on neural network. *Proceedings on Advances in Neural Networks - Isnn 2006, Part 3*, Vol. 3973, 2006, pp. 40-45.
11. Wu, J. and Tsai, Y. Enhanced roadway inventory using a 2-D sign video image recognition algorithm. *Computer-Aided Civil and Infrastructure Engineering*, Vol. 21, No. 5, 2006, pp. 369-382.
12. Liu, Y. X., T. Ikenaga, and S. Goto. Geometrical, physical and text/symbol analysis based approach of traffic sign detection system. *Ieice Transactions on Information and Systems*, Vol. E90d, No. 1, 2007, pp. 208-216.
13. Wu, J., and Tsai, Y. Real-time speed limit sign recognition based on locally adaptive thresholding and depth-first-search. *Photogrammetric Engineering and Remote Sensing*, Vol. 71, No. 4, 2005, pp. 405-414.
14. Bahlmann, C., Y. Zhu, R. Visvanathan, M. Pellkofer, and T. Koehler. A system for traffic sign detection, tracking, and recognition using color, shape, and motion information. Paper read at *Intelligent Vehicles Symposium 2005. Proceedings. IEEE*, 2005.
15. Silapachote, P., J. Weinman, A. Hanson, M. A. Mattar, and R. Weiss. Automatic Sign Detection and Recognition in Natural Scenes. Paper read at *IEEE Computer Society Conference on Computer Vision and Pattern Recognition Workshops*, 2005.
16. Tsai, Y., Kim, P. and Wang, Z. A Generalized Image Detection Model for Developing a Sign Inventory. *Journal of Computing in Civil Engineering* (In press), 2009.

17. Tsai, Y. and Wang, Z. Image Processing Algorithms for an Enhanced Roadway Sign Data Collection. Paper read at *Proceedings of the 7th international conference on managing pavement assets*, Calgary, Canada, 2008.
18. Canny, J. A Computational Approach to Edge Detection. , *IEEE Transactions on Pattern Analysis and Machine Intelligence*, Vol. 8, No. 6, 1986, pp. 679-698.
19. Abdou, I. E., and W. K. Pratt. Quantitative design and evaluation of enhancement/thresholding edge detectors. *Proceedings of the IEEE*, Vol. 67, No. 5, 1979, pp. 753-763.
20. Ames, W. F. Section 1.6 in *Numerical Methods for Partial Differential Equations*. Academic Press, New York, 1977.
21. Douglas, D. H., and T. K. Peucker. Algorithms for the reduction of the number of points required to represent a digitized line or its caricature. *The Canadian Cartographer*, Vol. 10, 1973, pp. 112-122.
22. Kass, M., A. Witkin, and D. Terzopoulos. Snakes: Active contour models. *International Journal of Computer Vision*, Vol. 1, No. 4, 1988, pp. 321-331.
23. Malladi, R., J. A. Sethian, and B. C. Vemuri. Shape modeling with front propagation: a level set approach. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, Vol. 17, No. 2, 1995, pp. 158-175.
24. Chenyang, X., and J. L. Prince. Snakes, shapes, and gradient vector flow. *IEEE Transactions on Image Processing*, Vol. 7, No. 3, 1998, pp. 359-369.
25. Chan, T. F., and L. A. Vese. Active contours without edges. *IEEE Transactions on Image Processing*, Vol. 10, No. 2, 2001, pp. 266-277.
26. Quan, L., and R. Mohr. Using Geodesic Model Guided Active Contour Method for Traffic Sign Detection. Paper read at *IAPR Conference on Machine Vision Applications*, Tokyo, 1990.
27. Paulo, C. F., and P. L. Correia. Traffic Sign Recognition Based on Pictogram Contours. Paper read at *Ninth International Workshop on Image Analysis for Multimedia Interactive Services*, 2008.
28. Andrade, E. L., S. Blunsden, and R. B. Fisher. Characterization of optical flow anomalies in pedestrian traffic. Paper read at *The IEE International Symposium on Imaging for Crime Detection and Prevention, ICDP 2005*, 2005.
29. Coifman, B., D. Beymer, P. McLauchlan, and J. Malik. A real-time computer vision system for vehicle tracking and traffic surveillance. *Transportation Research Part C-Emerging Technologies*, Vol. 6, No. 4, 1998, pp. 271-288.