

1 **A MOBILE CROSS SLOPE MEASUREMENT METHOD USING LIDAR**
2 **TECHNOLOGY**

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42 **ABSTRACT**

43 A properly measured, effective cross slope facilitates drainage on highways and prevents
44 hydroplaning. There is a need for transportation agencies to identify and measure road sections
45 that have improper and non-effective cross slopes so that timely corrective maintenance can be
46 performed. However, the traditional manual methods used by transportation agencies to measure
47 cross slope, i.e. using a digital level, are time-consuming and labor-intensive. They are not
48 feasible for conducting a network-level cross slope measurement. This research project,
49 sponsored by the United States Department of Transportation Research Innovative Technology
50 Administration (USDOT RITA) program, proposes a new mobile cross-slope measurement
51 method using emerging mobile LiDAR technology that can accurately and effectively conduct
52 network-level cross slope measurement at highway speed. The contributions of this paper
53 include the following: 1) proposing a mobile cross slope measurement method using emerging
54 LiDAR technology (LiDAR cloud calibration, data acquisition, ROI extraction, and cross slope
55 computation) ; 2) through a sensitivity study, determining the key parameter (i.e. the ROI
56 interval) for the proposed method; 3) critically validating the accuracy and the repeatability of
57 the proposed method by testing it in a controlled environment; and 4) conducting a case study to
58 demonstrate the capability of the proposed method. Experimental testing at the Georgia Tech
59 Savannah campus is first conducted to critically assess the accuracy and repeatability of
60 measuring cross slopes. When compared to the ground truth established by digital level, the
61 results from 15 cross slopes (ranging between 1.9% and 7.2%) show that the proposed method
62 can achieve desirable accuracy with an average measurement difference of 0.13% (i.e. 0.08°).
63 Results show that the proposed method can achieve a desirable level of repeatability with a
64 standard deviation of less than 0.05% (i.e. 0.03°) in three different test runs. A case study on
65 Interstate 285 is then conducted to demonstrate the capability of the proposed method for
66 achieving proper, effective, network-level cross slope measurements. Results show that the
67 proposed mobile method can be operated at highway speed and is very promising for a network-
68 level cross slope adequacy assessment. Finally, conclusions and recommendations are presented.

69 INTRODUCTION

70 The cross slope is a crucial roadway feature that accelerates water drainage and reduces potential
71 roadway hazards that cause hydroplaning. In addition, roadways are designed to slope in the
72 transverse direction to control lateral vehicle wandering, especially on curves, known as super-
73 elevation. Transportation agencies need to identify the potential for vehicle roadway departure or
74 hydroplaning by analyzing the roadway's cross slope features, along with other factors, e.g.
75 pavement surface friction, vertical grade, etc.

76 Most transportation agencies currently conduct cross slope measurement manually by
77 using a digital level (1, 2). This method requires field engineers to physically place a 4-foot
78 electronic level on the pavement surface to obtain the measurement. FIGURE 1 shows a field
79 engineer conducting manual measurement. Such manual measurement is time-consuming and
80 dangerous. More importantly, since it is not practical to conduct the manual measurement
81 continuously without traffic control, it is almost impossible for transportation agencies to collect
82 the cross slope data necessary to support a network-level analysis for identifying safety concerns,
83 such as potential hydroplaning locations, inadequate super-elevated locations, etc.



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FIGURE 1 Manual cross slope measurement (3).

86 Light detection and ranging (LiDAR) technology has become popular among
87 transportation agencies for asset data collections (4, 5), traffic data collection (6), safety
88 assessment (7), etc. In recent years, mobile LiDAR has been increasingly used for roadside
89 inventory (8), roadway geometry measurement (9-11), etc. With accurate geo-referenced 3D
90 point cloud data and a high-scanning frequency, the mobile LiDAR technology has the potential
91 to achieve safer and more effective cross slope measurements at highway speed. Such
92 measurements can be extracted from a LiDAR point cloud.

93 Although some researchers have introduced other sensing technologies to facilitate a
94 mobile cross slope measurement method, such as airborne LiDAR (12), laser profiler and inertial
95 measurement unit (IMU) (13), etc., mobile LiDAR technology has never been practically used
96 for mobile cross slope measurement. This study proposes a new mobile cross slope measurement
97 method using mobile LiDAR; it critically evaluates the accuracy and repeatability of the
98 proposed method by using actual data collected on the Georgia Tech Savannah campus in
99 Savannah, Georgia. A case study is presented to demonstrate the network-level analysis
100 capability of the proposed method by using the actual data collected on Interstate 285 (I-285) in
101 Atlanta, Georgia.

102 This paper is organized as follows. The first section identifies the research need and
103 objective. The second presents the proposed mobile cross slope measurement method using

104 mobile LiDAR. The third section presents a critical assessment conducted to validate the
 105 accuracy and repeatability of the proposed method. The fourth section uses a case study to
 106 demonstrate the capability of the proposed method.

107 **PROPOSED CROSS SLOPE MEASUREMENT METHOD USING MOBILE LIDAR**

108 **Proposed Method**

109 In this section, a mobile cross slope measurement method is proposed. The method uses Georgia
 110 Tech's mobile sensing system, which can collect the data at highway speed. The integrated
 111 system includes an emerging mobile LiDAR system (i.e. Riegl LMS-Q120i), high resolution
 112 video cameras (i.e. Point Grey Gras-50S5C), and an accurate positioning system (i.e. Applanix
 113 LV 210PP) composed of a global positioning system (GPS), an IMU, and a distance
 114 measurement instrument (DMI). FIGURE 2(a) shows the mobile LiDAR system and the two
 115 corresponding cameras; the rest of the system components are enclosed in the data collection
 116 vehicle.

117 The mobile LiDAR system in this study is a line-scanning laser device that produces
 118 10,000 laser points per second. As the vehicle moves in the longitudinal direction on the road,
 119 the scanning line of the LiDAR system is aligned parallel to the transverse direction. The
 120 scanning range is 80° in the horizontal direction, which produces an 80° fan covering the
 121 pavement surface. Currently, the frequency of the LiDAR system is configured at 100 Hz with
 122 100 points in each scan. FIGURE 2(b) illustrates data acquisition covering the whole driving
 123 lane.

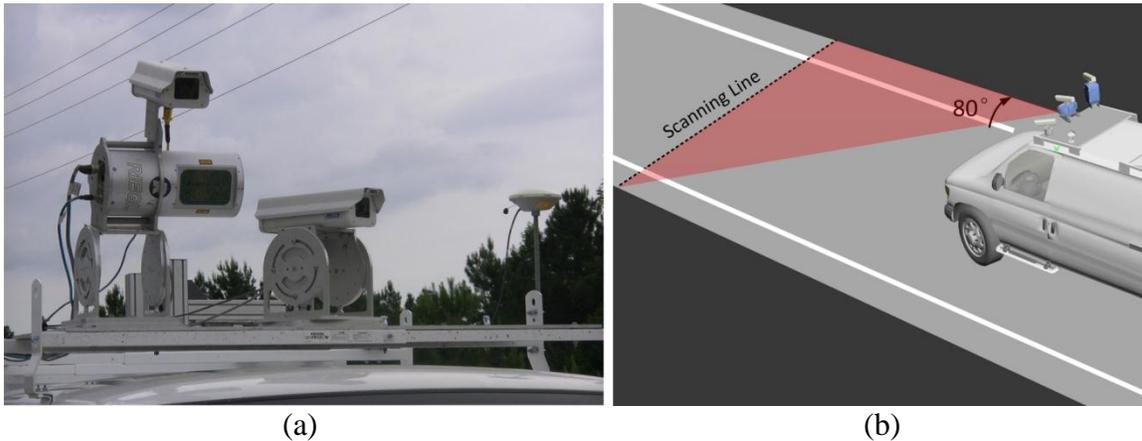
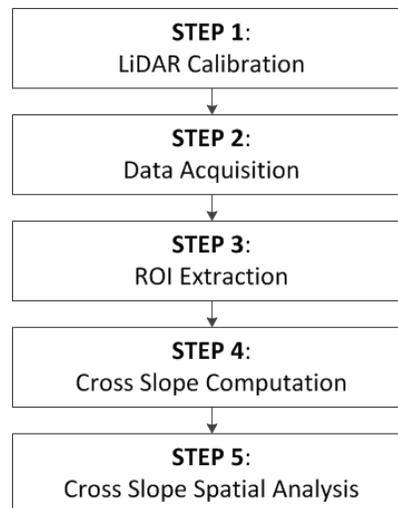


FIGURE 2 Illustration for data acquisition using LiDAR.

127 The proposed method for cross slope measurement using mobile LiDAR contains five primary
 128 steps, including LiDAR calibration, data acquisition, region of interest (ROI) extraction, cross
 129 slope computation, and cross slope spatial analysis. FIGURE 3 shows the flow of the proposed
 130 method using mobile LiDAR.



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FIGURE 3 Flowchart of the propose cross slope measurement method

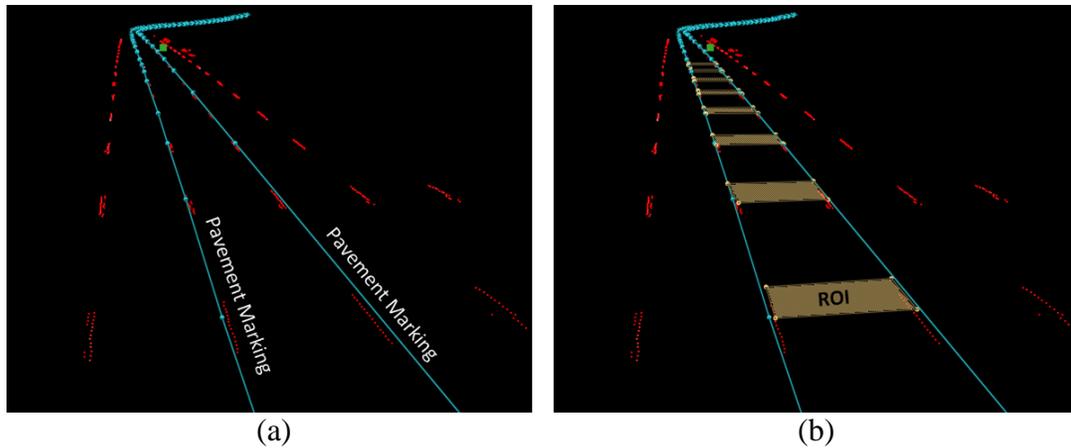
133 **STEP 1:** LiDAR calibration. LiDAR calibration is conducted to determine the relative positions
134 (i.e. offsets to the GPS antenna in x, y, and z directions) and the actual orientation (i.e. heading,
135 rolling, and pitching angles) of the data collection system components. The calibration results
136 will be used for point cloud data computation. Sensor calibration needs to be conducted only
137 when the sensor configuration is changed.

138 **STEP 2:** Data acquisition. Data acquisition is collected for the testing dataset using the
139 calibrated mobile LiDAR. The raw LiDAR point cloud collected at highway speed contains only
140 the beam distance and beam angle. The raw LiDAR point cloud needs to be post processed using
141 the calibration results and the high accuracy GPS/IMU system (14).

142 **STEP 3:** ROI extraction. ROI extraction is performed on the collected LiDAR point cloud to
143 extract the rectangular region within a single lane between the pavement markings. Individual
144 cross slope measurement will be conducted within each ROI. FIGURE 4 shows an example of
145 the ROI for individual cross slope measurement in this study. The ROI can be extracted in two
146 sub-steps, which correspond to the two dimensions of the defined ROI:

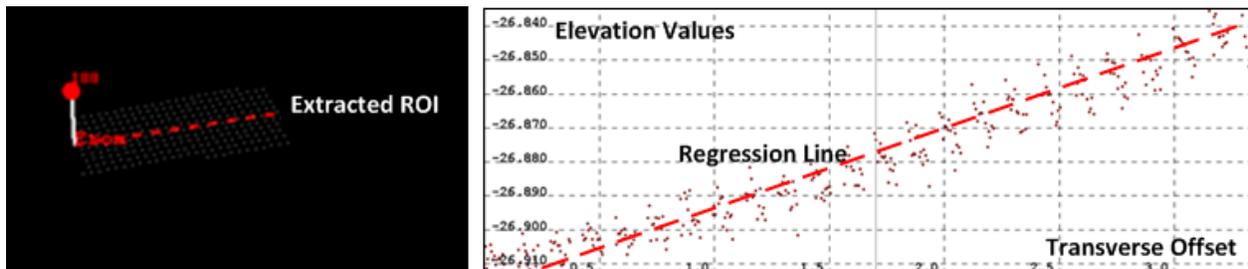
147 STEP 3.1: Pavement marking extraction (ROI width in transverse direction). The width of
148 the ROI is defined by the distance between the pavement markings. The pavement markings
149 can be automatically or semi-automatically extracted from video log images based on the
150 existing pavement marking extraction algorithm (15) or from LiDAR point cloud (16, 11). In
151 this study, the semi-automatic pavement marking extraction method using the LiDAR point
152 cloud is used. FIGURE 4(a) shows the pavement marking extraction result, where the red
153 dots are the extracted pavement marking from the LiDAR point cloud, and the blue line is the
154 connected pavement marking.

155 STEP 3.2: ROI interval determination (ROI length in longitudinal direction). ROI interval is
156 the key parameter that impacts the accuracy of cross slope computation because it determines
157 the size of the buffer for the regression in the next step. The detailed sensitivity study is
158 presented in the following section. FIGURE 4(b) shows an example of the extracted ROI
159 with an interval of 8ft.



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162 **FIGURE 4 Example of the ROI extraction for individual cross slope measurement.**

163 **STEP 4:** Cross slope computation. For each extracted ROI, a small group of LiDAR points are
164 extracted for cross slope computation. As each of the LiDAR points incorporates the accuracy of
165 GPS information, including the elevation value in z direction, a linear regression for the
166 association between the extracted elevations and the transverse offset of the lane is conducted.
167 Therefore, the slope of the regression result represents the cross slope within the corresponding
168 ROI. FIGURE 5 shows an illustration of the extracted points from an extracted ROI and the
169 corresponding elevation values for linear regression.



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171 **FIGURE 5 Illustration of the extracted point within an ROI for regression.**

172 **STEP 5:** Cross slope spatial analysis. After all of the cross slope measurements are computed in
173 the tested road section, each measurement from the corresponding ROI is represented by a single
174 geo-referenced point (i.e. the centroids for each ROI). A geo-database can be generated
175 containing the GPS coordinates with all of the cross slope measurements. Such a database can be
176 integrated with other databases with pavement geometry measurements (e.g. curvature, vertical
177 grade, etc.) or pavement surface conditions (e.g. rutting, raveling, etc.) so that a network-level
178 spatial analysis can be conducted to identify potential hydroplaning locations, inadequate super-
179 elevated locations, etc.

180 **CRITICAL ASSESSMENT OF THE PROPOSED METHOD**

181 The objective of the critical assessment is to assess the accuracy and repeatability of the
182 proposed method using mobile LiDAR. Actual data collected on Georgia Tech's Savannah
183 campus and from Jimmy Deloach Parkway and Pooler Parkway in Savannah, Georgia, are used
184 for the accuracy and repeatability assessment.

185 The dataset collected for the accuracy and repeatability assessment contains 15
 186 distinctive cross slope measurement locations. The benchmarked cross slopes are measured using
 187 the digital level with 0.1° accuracy, which is typically used by transportation agencies. The
 188 benchmarked values range between 1.9% and 7.2%; these cover the most frequent cross slope
 189 values and some super-elevated curves. The dataset collected for the case study covers 3 miles of
 190 I-285 with three horizontal curves. After the establishment of the ground truth using a digital
 191 level, Georgia Tech's mobile sensing system collected the LiDAR data at 30 mph.

192 Sensitivity Study of the ROI Interval

193 As presented in previous section, the key parameter used for the cross slope computation is the
 194 selection of the ROI interval. Since the cross slope is computed based on the regression result of
 195 the LiDAR point's elevation, there is a trade-off in selecting the ROI interval. With a small
 196 interval, fewer LiDAR points are included in the ROI, so a single outlier could impact the whole
 197 result. With a large interval, more LiDAR points are included in the ROI, but pavement
 198 fluctuation could change the elevation within the ROI, which might introduce computation error.
 199 In this sub-section, the sensitivity study of the ROI interval is conducted to determine the
 200 appropriate ROI interval for the analysis.

201 Three testing locations are selected for the sensitivity study to determine an adequate
 202 interval to compute the cross slope. The testing locations include different cross slope values and
 203 vertical grade values. TABLE 1 shows the testing locations' information.

204 **TABLE 1 Testing locations for the ROI interval sensitivity study**

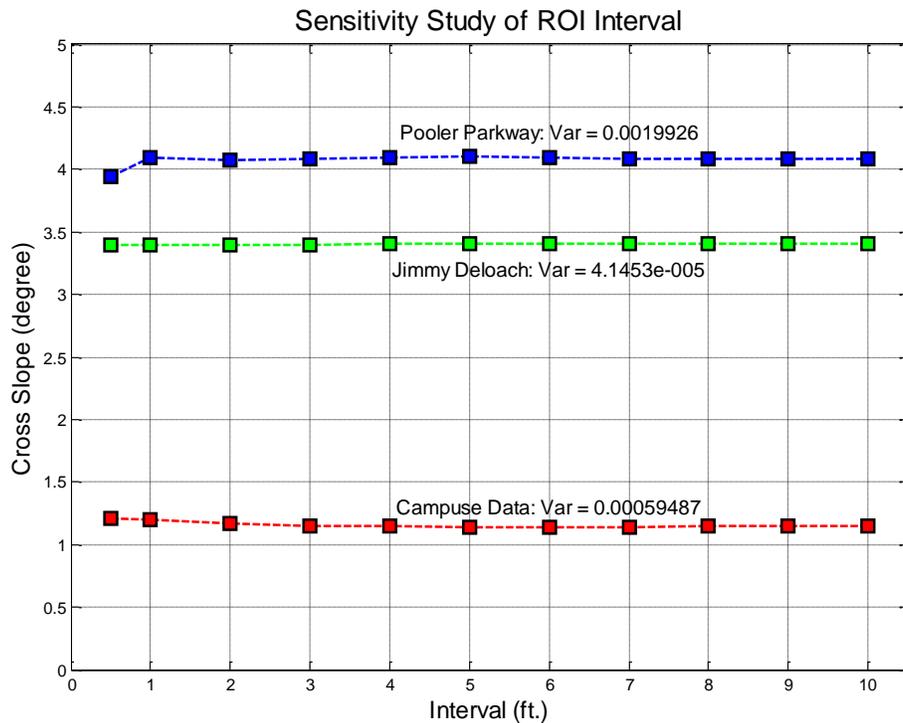
	Cross Slope	Vertical Grade	Latitude	Longitude
Georgia Tech Savannah Campus	1.2°	0°	32.170147	-81.209872
Jimmy Deloach Parkway	3.4°	2°	32.168187	-81.219250
Pooler Parkway	4.1°	0°	32.140480	-81.249285

205 Eleven intervals, 0.5ft., 1ft., 2ft., 3ft., 4ft., 5ft., 6ft., 7ft., 8 ft., 9ft. and 10 ft., were used for each
 206 location to assess the sensitivity of the proposed measurement method. No ROI interval smaller
 207 than 0.5 ft. was tested because the longitudinal interval of the LiDAR point cloud is about 0.5 ft.
 208 when driving at 30mph during the data collection. FIGURE 6 shows the results of the proposed
 209 method using different ROI intervals. The result shows several key points for interval selection,
 210 including

- 211 • When the interval is greater or equal to 2 ft., the cross slope measurement results stabilize,
 212 regardless of the actual cross slope value (i.e. $1.2^\circ \sim 4.1^\circ$);
- 213 • The cross slope measurement results are not sensitive to the change of the tested ROI
 214 interval, regardless of the vertical grade up to 2° (i.e. the data collected on Jimmy Deloach
 215 Parkway contains a vertical grade of approximated 2°);
- 216 • The cross slope measurement results are sensitive when a small interval is selected because
 217 the regression result is sensitive to the outliers when fewer LiDAR points are included in the
 218 ROI for regression.
 - 219 ○ The cross slope was underestimated on Pooler Parkway when using 0.5 ft. as the ROI
 220 interval (i.e. blue plot in FIGURE 6). A further investigation revealed that the pavement
 221 contains several missing stones close to the center, which slightly decreases the computed
 222 value.

- The cross slope was slightly overestimated on the Georgia Tech Savannah campus when using 0.5ft. and 1ft. as the ROI intervals (i.e. red plots in FIGURE 6). A further investigation revealed that the pavement contains small fluctuations near the outside edge of the pavement, which slightly increased the computed value.

It was learned from the sensitivity study that an ROI interval of 2ft. is adequate for the proposed mobile cross slope measurement method at 30 mph. Although other ROI intervals that are greater than 2ft. can still be used for the proposed method with a consistent result, the ROI interval of 2ft. is used in this study to preserve the densest cross slope measurements. In addition, as different LiDAR models or data collection speeds can be used by different transportation agencies, the adequate ROI interval could change. Nevertheless, following the similar sensitivity study procedure, the adequate ROI interval for different transportation agencies can be determined.



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FIGURE 6 Results of the sensitivity study on the ROI interval.

237 Assessment of the Proposed Method

238 With the adequate ROI interval, i.e. 2 ft., the datasets collected on the Georgia Tech Savannah
239 campus and from Jimmy Deloach Parkway and Pooler Parkway were tested using the proposed
240 method. TABLE 2 shows the measurement results.

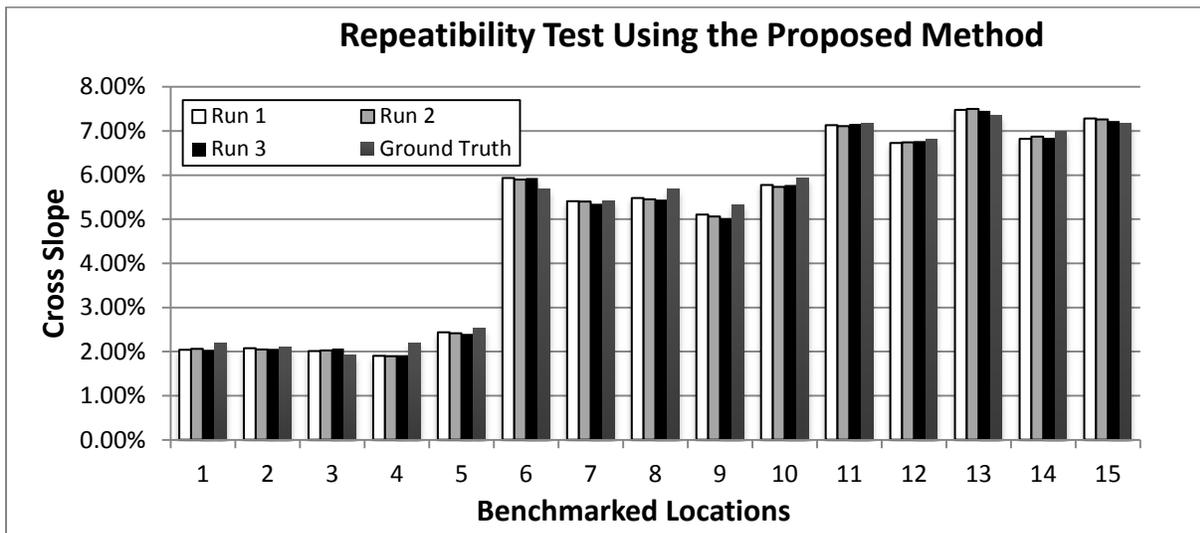
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TABLE 2 Assessment results of the cross slope measurement accuracy

	Ground Truth (%)	Proposed Method		Absolute Difference (%)	Relative Difference (%)
		Mean (%)	STDev (%)		
GT Savannah	2.18%	2.06%	0.02%	0.13%	5.77%
campus	2.09%	2.07%	0.02%	0.02%	1.02%
	1.92%	2.04%	0.02%	-0.12%	-6.08%

	2.18%	1.89%	0.02%	0.30%	13.52%
	2.53%	2.39%	0.03%	0.14%	5.48%
Jimmy Deloach	5.68%	5.92%	0.02%	-0.24%	-4.20%
Parkway	5.42%	5.37%	0.03%	0.04%	0.81%
	5.68%	5.44%	0.02%	0.23%	4.14%
	5.33%	5.03%	0.05%	0.29%	5.50%
	5.94%	5.78%	0.03%	0.16%	2.76%
Pooler	7.17%	7.16%	0.04%	0.01%	0.17%
Parkway	6.82%	6.75%	0.02%	0.07%	0.96%
	7.34%	7.46%	0.03%	-0.12%	-1.61%
	6.99%	6.84%	0.02%	0.16%	2.23%
	7.17%	7.24%	0.03%	-0.07%	-1.04%

242 The cross slope measurements at the 15 benchmarked locations derived from the proposed
 243 method were compared to those measured using a digital level with 0.1° accuracy. At each
 244 benchmarked location, the ground truth was measured twice, and the measurements were
 245 averaged. TABLE 2 shows that the derived measurements are very close to the ones measured
 246 using the digital level; there is a maximum difference of 0.28% cross slope (i.e. 0.17°) and an
 247 average difference less than 0.13% cross slope (i.e. 0.08°). No bias is observed from the results.
 248 From the results, it is identified that the derived cross slope measurements achieve a desirable
 249 accuracy, considering the instrumentation accuracy for the digital level is only 0.1°, which is
 250 used by many transportation agencies (1, 2).
 251 The repeatability of the measurements at the 15 benchmarked locations was also studied by
 252 conducting the data collection in three different runs. FIGURE 7 shows derived cross slope
 253 measurement from the three runs. As shown in FIGURE 7 and TABLE 2, there is no significant
 254 difference observed among different runs. The standard deviations are within 0.05% (i.e. 0.03°)
 255 at all benchmarked locations. The results show that the derived cross slope measurements using
 256 the proposed method are consistent and repeatable in different runs.



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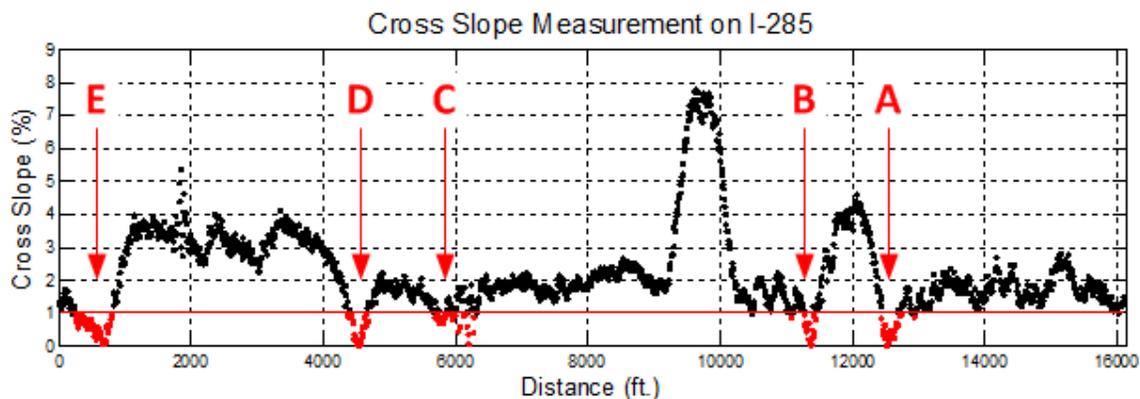
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FIGURE 7 Assessment results of the cross slope measurement repeatability.

259 Based on the accuracy and repeatability test using the actual data collected on the Georgia Tech
 260 Savannah campus and Jimmy Deloach Parkway and Pooler Parkway in Savannah, Georgia, the
 261 results have demonstrated that the proposed method can measure the cross slope with an average
 262 measurement error of less than 0.08° and a measurement standard deviations of less than 0.05%.
 263 Many state DOTs, such as Texas DOT (2), Florida DOT (3), etc., require that the measurement
 264 error of the cross slope measurement be 0.1° , and the measurement standard deviation is 0.2%.

265 CASE STUDY: INTERSTATE 285

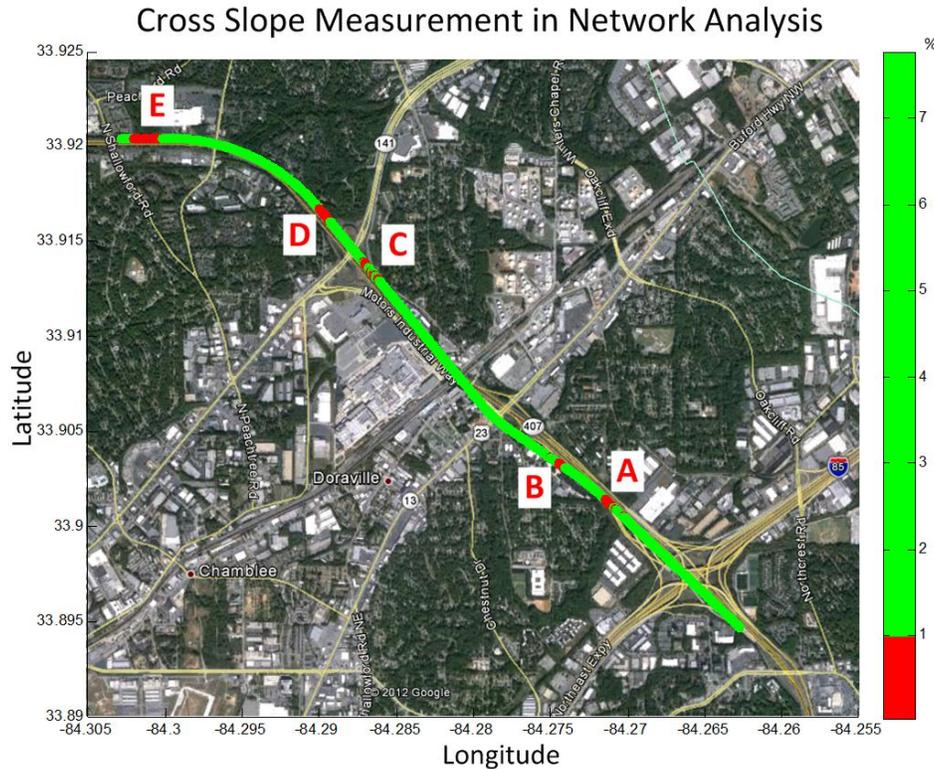
266 The objective of the case study is to demonstrate the capability of using the proposed method for
 267 a network-level cross slope measurement. Georgia Tech's sensing vehicle was used to collect the
 268 data at highway speed (i.e. 60mph) on the outside lane of I-285 from MP30 to MP33. The cross
 269 slope measurements are aggregated at every 10ft in the longitudinal direction; data was obtained
 270 using the proposed method by computing cross slope at every 2ft. FIGURE 8 shows all the
 271 measurements from the testing section. Engineers can identify the five sections (i.e. the red
 272 sections of A-E in FIGURE 8) with cross slopes less than 1.0% (i.e. sub-standard) that need to
 273 have a site visit for close assessment.



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FIGURE 8 Network-level cross slope measurement on I-285.

276 After the computation, since each cross slope measurement corresponds with a unique GPS
 277 coordinate, the cross slope measurement, as shown in FIGURE 8, can be plotted onto a GIS map
 278 where the cross slope values can be represented using different colors. FIGURE 9 shows an
 279 example of the representation of the results. The red portion displayed in the GIS map
 280 corresponds to the locations where cross slope is less than 1%. This information is very useful
 281 for transportation agencies. For example, engineers can use this cross slope GIS map to identify
 282 the sub-standard cross slope locations (i.e. less than 1.0%) for a focused assessment (e.g. a site
 283 visit). In addition, the GIS-based cross slope measurement results can be used to support
 284 network-level roadway safety assessment by incorporating them with other measurements, such
 285 as vertical grade measurements, curvatures, etc. This case study has demonstrated that the
 286 proposed method is very promising because it is capable of conducting a network-level cross
 287 slope measurements at highway speed, which will support roadway safety analysis.



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FIGURE 9 GIS-based cross slope measurement analysis on I-285.

290 CONCLUSIONS AND RECOMMENDATIONS

291 The cross slope is a critical roadway feature that facilitates water drainage and reduces the
 292 potential of hydroplaning. It is important for transportation agencies to identify road sections
 293 with poor, ineffective, and sub-standard cross slopes that require correction. However, the
 294 current practice for cross slope measurement is conducted manually, which is time-consuming,
 295 labor-intensive, and ineffective. Some automated technologies have been proposed for cross
 296 slope measurement using airborne LiDAR (12), laser profiler and inertial measurement unit
 297 (IMU) (13), etc. However, none of these technologies have been practically used, and their
 298 accuracy and repeatability have not been quantitatively assessed. In this study, a new mobile
 299 cross slope measurement method using the emerging mobile LiDAR technology is proposed to
 300 address the need of transportation agencies for a mobile, cost-effective network-level cross slope
 301 measurement method. The accuracy and repeatability of the proposed methods are quantitatively
 302 assessed and compared with the current cross slope measurement methods that are commonly
 303 used in state DOTs. The proposed method provides a better measurement accuracy and
 304 repeatability. The following points summarize the major findings of this study:

- 305 • Based on critical assessment, results show that the proposed method is very promising; it can
 306 achieve a desirable measurement accuracy with a maximum difference of 0.28% cross slope
 307 (i.e. 0.17°) and an average difference less than 0.13% cross slope (i.e. 0.08°) on the tested
 308 sections with cross slopes ranging between 1.9% and 7.2%. The acceptable accuracy is
 309 typically 0.2% (or 0.1°) during the construction quality control (3).
- 310 • Repeatability assessment results show the proposed method can achieve a good repeatability
 311 with the standard deviations within 0.05% (i.e. 0.03°) at 15 different benchmarked locations

312 in three different runs. The acceptable repeatability is typically 0.2% during the construction
313 quality control (3).

- 314 • The case study on I-285 has demonstrated that the proposed method has the capability to
315 conduct network-level analysis efficiently. The GIS-based cross slope measurement map of
316 the 3-mile section of roadway that was studied can be derived in less than 2 man hours using
317 the collected raw LiDAR data.

318 The following are the recommendations for future research:

- 319 • Additional datasets with different roadway environments should be used for further
320 assessment of the performance of the proposed method. Using the proposed method to study
321 of the impacts of a non-uniform cross slope (e.g. ruttings, drop-offs, parabolic cross slopes,
322 etc.) on the measurement results is recommended.
- 323 • Further study should be undertaken to establish the relationship between the ROI interval and
324 the data collection speed, the LiDAR model, the pavement condition, etc., to provide a
325 reliable guideline for transportation agencies.
- 326 • A fully automatic pavement marking extraction algorithm is recommended to improve the
327 performance of the ROI extraction in the proposed method.
- 328 • Further comparison study of cost-effectiveness between the existing technologies and the
329 proposed method is recommended.

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